

# Z Reference Card

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## Specifications

### Schema box

Name[Params]	<code>\begin{schema}{Name}[Params]</code>
<i>Declarations</i>	Declarations
<i>Predicates</i>	<code>\where</code> Predicates <code>\end{schema}</code>

### Axiomatic description

<i>Declarations</i>	<code>\begin{axdef}</code>
<i>Predicates</i>	Declarations <code>\where</code> Predicates <code>\end{axdef}</code>

### Generic definition

<code>[Params]=====</code>	<code>\begin{gendef}[Params]</code>
<i>Declarations</i>	Declarations
<i>Predicates</i>	<code>\where</code> Predicates <code>\end{gendef}</code>

```
\begin{schema}{Name}[Params]
  Declarations
  \where
  Predicates
\end{schema}
```

```
\begin{axdef}
  Declarations
  \where
  Predicates
\end{axdef}
```

```
\begin{gendef}[Params]
  Declarations
  \where
  Predicates
\end{gendef}
```

`\begin{zed} ...`

### Basic type definition

`[NAME, DATE]` [NAME, DATE]

### Abbreviation definition

`DOC == seq CHAR` DOC == `\seq CHAR`

### Constraint

`n_disks < 5` n\_disks < 5

### Schema definition

`Point ≡ [x, y : Z]` Point `\defs [~x, y: \num~]`

### Free type definition

`Ans ::= ok⟨Z⟩ | error` Ans ::= ok `\ldata\num\rdata` | error  
`... \end{zed}`

## Logic and schema calculus

<i>true, false</i>	<i>true, false</i>	Logical constants
$\neg P$	$\text{\lnot } P$	Negation
$P \wedge Q$	$P \text{\land } Q$	Conjunction
$P \vee Q$	$P \text{\lor } Q$	Disjunction
$P \Rightarrow Q$	$P \text{\implies } Q$	Implication
$P \Leftrightarrow Q$	$P \text{\iff } Q$	Equivalence
$\forall x : T \mid P \bullet Q$	$\text{\forallall } ...$	Universal quantifier
$\exists x : T \mid P \bullet Q$	$\text{\existsexists } ...$	Existential quantifier
$\exists_1 x : T \mid P \bullet Q$	$\text{\existsexists}_1 ...$	Unique quantifier

## Special schema operators

$S[y_1/x_1, y_2/x_2]$	$S[y\_1/x\_1, y\_2/x\_2]$	Renaming
$S \setminus (x_1, x_2)$	$S \text{\hide } (x\_1, x\_2)$	Hiding
$S1 \upharpoonright S2$	$S1 \text{\project } S2$	Projection
$\text{pre } Op$	$\text{\pre } Op$	Pre-condition
$Op1 ; Op2$	$Op1 \text{\semi } Op2$	Sequential composition
$Op1 \gg Op2$	$Op1 \text{\pipe } Op2$	Piping

## Basic expressions

$x = y$	$x = y$	Equality
$x \neq y$	$x \neq y$	Inequality
$\text{if } P \text{ then } E_1$	$\text{\textbackslash IF } P \text{ \textbackslash THEN } E_1$	Conditional
$\text{else } E_2$	$\text{\textbackslash ELSE } E_2$	Expression
$\theta S$	$\text{\textbackslash theta } S$	Theta-expression
$E.x$	$E.x$	Selection
$(\mu x : T \mid P \bullet E)$	$(\text{\textbackslash mu } x : T \mid P \text{ @ } E)$	Mu-expression
$(\text{let } x == E_1 \bullet E_2)$	$(\text{\textbackslash LET } x == E_1 \text{ @ } E_2)$	Let-expression

## Sets

$x \in S$	$x \in S$	Membership
$x \notin S$	$x \notin S$	Non-membership
$\{x_1, \dots, x_n\}$	$\{x_1, \dots, x_n\}$	Set display
$\{x : T \mid P \bullet E\}$	$\{x : T \mid P \text{ @ } E\}$	Set comprehension
$\emptyset$	$\text{\textbackslash emptyset}$	Empty set
$S \subseteq T$	$S \subseteq T$	Subset relation
$S \subset T$	$S \subset T$	Proper subset relation
$\mathbb{P} S$	$\text{\textbackslash power } S$	Power set
$\mathbb{P}_1 S$	$\text{\textbackslash power\_1 } S$	Non-empty subsets
$S \times T$	$S \times T$	Cartesian product
$(x, y, z)$	$(x, y, z)$	Tuple
$\text{first } p$	$\text{first}^{\sim} p$	First of pair
$\text{second } p$	$\text{second}^{\sim} p$	Second of pair
$S \cup T$	$S \cup T$	Set union
$S \cap T$	$S \cap T$	Set intersection
$S \setminus T$	$S \setminus T$	Set difference
$\bigcup A$	$\text{\textbackslash bigcup } A$	Generalized union
$\bigcap A$	$\text{\textbackslash bigcap } A$	Generalized intersection
$\mathbb{F} X$	$\text{\textbackslash finset } X$	Finite sets
$\mathbb{F}_1 X$	$\text{\textbackslash finset\_1 } X$	Non-empty finite sets

## Relations

$X \leftrightarrow Y$	$X \text{ \textbackslash rel } Y$	Binary relations
$x \mapsto y$	$x \text{ \textbackslash mapsto } y$	Maplet
$\text{dom } R$	$\text{\textbackslash dom } R$	Domain
$\text{ran } R$	$\text{\textbackslash ran } R$	Range
$\text{id } X$	$\text{\textbackslash id } X$	Identity relation
$Q ; R$	$Q \text{ \textbackslash comp } R$	Composition
$Q \circ R$	$Q \text{ \textbackslash circ } R$	Backwards composition
$S \triangleleft R$	$S \text{ \textbackslash dres } R$	Domain restriction
$R \triangleright S$	$R \text{ \textbackslash rres } S$	Range restriction
$S \triangleleft\! R$	$S \text{ \textbackslash ndres } R$	Domain anti-restriction
$R \triangleright\! S$	$R \text{ \textbackslash nrres } S$	Range anti-restriction
$R^\sim$	$R \text{ \textbackslash inv}$	Relational inverse
$R(S)$	$R \text{ \textbackslash limg } S \text{ \textbackslash rimg}$	Relational image
$Q \oplus R$	$Q \text{ \textbackslash oplus } R$	Overriding
$R^k$	$R^{\sim k}$	Iteration
$R^+$	$R \text{ \textbackslash plus}$	Transitive closure
$R^*$	$R \text{ \textbackslash star}$	Reflexive-trans. closure

## Functions

$f(x)$	$f(x)$	Function application
$(\lambda x : T \mid P \bullet E)$	$(\text{\textbackslash lambda } \dots)$	Lambda-expression
$X \rightarrowtail Y$	$X \text{ \textbackslash pfun } Y$	Partial functions
$X \rightarrow Y$	$X \text{ \textbackslash fun } Y$	Total functions
$X \rightarrowtail\! Y$	$X \text{ \textbackslash pinj } Y$	Partial injections
$X \rightarrow\! Y$	$X \text{ \textbackslash inj } Y$	Total injections
$X \rightarrowtail Y$	$X \text{ \textbackslash psurj } Y$	Partial surjections
$X \rightarrow\! Y$	$X \text{ \textbackslash surj } Y$	Total surjections
$X \rightarrowtail\! Y$	$X \text{ \textbackslash bij } Y$	Bijections
$X \rightarrowtail Y$	$X \text{ \textbackslash ffun } Y$	Finite partial functions
$X \rightarrowtail\! Y$	$X \text{ \textbackslash finj } Y$	Finite partial injections

## Numbers and arithmetic

$\mathbb{N}$	<code>\nat</code>	Natural numbers
$\mathbb{Z}$	<code>\num</code>	Integers
$+ - * \text{div} \text{mod}$	<code>+ - * \div \mod</code>	Arithmetic operations
$< \leq \geq >$	<code>&lt; \leq \geq &gt;</code>	Arithmetic comparisons
$\mathbb{N}_1$	<code>\nat_1</code>	Strictly positive integers
$\text{succ}$	<code>\succc</code>	Successor function
$m .. n$	<code>m \upto n</code>	Number range
$\#S$	<code>\# S</code>	Size of a set
$\min S$	<code>\min^S</code>	Minimum of a set
$\max S$	<code>\max^S</code>	Maximum of a set

## Bags

$\text{bag } X$	<code>\bag X</code>	Bags
$\llbracket x_1, \dots, x_n \rrbracket$	<code>\lbag ... \rbag</code>	Bag display
$\text{count } B\ x$	<code>\count^B x</code>	Count of an element
$B \# x$	<code>B \bcount x</code>	Infix count operator
$n \otimes B$	<code>n \otimes B</code>	Bag scaling
$x \in B$	<code>x \inbag B</code>	Bag membership
$B \sqsubseteq C$	<code>B \subageq C</code>	Sub-bag relation
$B \uplus C$	<code>B \uplus C</code>	Bag union
$B \ominus C$	<code>B \uminus C</code>	Bag difference
$\text{items } s$	<code>\items^s</code>	Items in a sequence

## Sequences

$\text{seq } X$	<code>\seq X</code>	Finite sequences
$\text{seq}_1 X$	<code>\seq_1 X</code>	Non-empty sequences
$\text{iseq } X$	<code>\iseq X</code>	Injective sequences
$\langle x_1, \dots, x_n \rangle$	<code>\langleangle ... \rangleangle</code>	Sequence display
$s \hat{t}$	<code>s \cat t</code>	Concatenation
$\text{rev } s$	<code>\rev s</code>	Reverse
$\text{head } s$	<code>\head s</code>	Head of sequence
$\text{last } s$	<code>\last s</code>	Last element of sequence
$\text{tail } s$	<code>\tail s</code>	Tail of sequence
$\text{front } s$	<code>\front s</code>	All but last element
$U \upharpoonright s$	<code>U \extract s</code>	Extraction
$s \upharpoonright V$	<code>s \filter V</code>	Filtering
$\text{squash } f$	<code>\squash^f</code>	Compaction
$s \text{ prefix } t$	<code>s \prefix t</code>	Prefix relation
$s \text{ suffix } t$	<code>s \suffix t</code>	Suffix relation
$s \text{ in } t$	<code>s \inseq t</code>	Segment relation
$\wedge/ss$	<code>\dcat ss</code>	Distributed concat.
$\text{disjoint } SS$	<code>\disjoint SS</code>	Disjointness
$SS \text{ partition } T$	<code>SS \partition T</code>	Partition relation

## fuzz flags

Usage: `fuzz [-aqstv] [-p prelude] [file ...]`

<code>-a</code>	Don't use type abbreviations
<code>-p prelude</code>	Use <code>prelude</code> in place of the standard one
<code>-q</code>	Assume implicit quantifiers for undeclared variables
<code>-d</code>	Dependency analysis
<code>-s</code>	Syntax check only
<code>-t</code>	Report types of global definitions
<code>-v</code>	Echo formal text as it is parsed